| 科目ナンバリング U-LAS10 20006 LE55 |               |      |                              |        |     |              |                    |      |      |                     |     |    |
|-----------------------------|---------------|------|------------------------------|--------|-----|--------------|--------------------|------|------|---------------------|-----|----|
| 授業科目 (英訳>                   |               |      | near Algebra<br>near Algebra |        |     | 担当者所<br>戦名・氏 | 当者所属<br>名・氏名 工学研究科 |      |      | 准教授 CHANG, Kai-Chun |     |    |
| 群                           | 自然科学          | 学科目群 | <u> </u>                     | 分野(分類) | 数学( |              |                    |      |      | 用言語                 | 英語  |    |
| 旧群                          | B群            | 単位数  | 2単位                          | 週コマ数   | 133 | ₹            | 授業                 | 形態 誹 | 義    | 義(対面授業科目)           |     | 目) |
| 開講年度・<br>開講期                | 2025・前期 曜時限 3 |      |                              | 2      | 配当  | 配当学年 主として2   |                    | 2回生  | 対象学生 |                     | 理系向 |    |

## [授業の概要・目的]

Linear Algebra is a fundamental tool commonly used in many fields, not only in mathematics but also in the natural sciences, engineering, and more. This course builds on the contents in "Linear Algebra A/B" courses (majorly provided for 1st-year students) and explores advanced concepts of linear algebra, such as orthogonality, diagonalization, Singular Value Decomposition (SVD) of matrices, Jordan canonical form, and their applications to real-world problems.

## [到達目標]

- To acquire an understanding of advanced concepts in linear algebra, such as orthogonality, diagonalization, and SVD of matrices.
- To understand and apply linear algebra concepts to solve real-world problems.

## [授業計画と内容]

- 1. Review of linear algebra [2 weeks]
- Big picture, rank, dimension, LU/LDU factorization, Gauss-Jordan elimination, etc.
- vector spaces, subspaces, nullspace, complete solutions, four subspaces and their dimensions and orthogonality, etc.
- 2. Orthogonality and its applications [4 weeks]
- Orthogonality and orthogonality complement, projections, least square approximations, orthogonal bases, Gram-Schumidt process, etc.
- 3. Eigenvalues, eigenvectors, and their applications [4 weeks]
- Eigenvalues and eigenvectors, diagonalization, matrix power, singular value decomposition (SVD) and their application to difference equations, differential equations and Markov process, etc.
- 4. Jordan canonical form [3 weeks]
- minimal polynomials, generalized eigenvectors, Jordan canonical form, and their applications.
- 5. Optional topics [1 week]
- numerical solutions, complex vectors and matrices, other applications, etc.
- 6. Feedback [1 week]

#### [履修要件]

Suggested prerequisites: Calculus A/B and Linear Algebra A/B, or Calculus with Exercises A/B and Linear Algebra with Exercises A/B.

Advanced Linear Algebra(2)へ続く

# Advanced Linear Algebra(2) [成績評価の方法・観点] Quizzes or assignments (50%); final examination (50%) [教科書] Handouts distributed in class or uploaded to PandA [参考書等] (参考書) Strang, G. (2009) F Introduction to Linear Algebra. 5th ed. (Wellesley-Cambridge Press) Lipschutz, S. and Lipson, M. (2012) Linear Algebra, 6th ed. (McGraw-Hill) [授業外学修(予習・復習)等] Students are expected to dedicate at least 2 hours per week to preview and review. More than half of this time is spent preparing for class and completing assignments. [その他(オフィスアワー等)] Any inquiry to the instructor: chang.kaichun.4z{at}kyoto-u.ac.jp. (replace {at} with @) [主要授業科目(学部・学科名)] 理学部